

# **Analytical Calculation of Helicopter Main Rotor Blade Flight Loads in Hover and Forward Flight**

by Ki C. Kim

ARL-TR-3180 April 2004

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# **Analytical Calculation of Helicopter Main Rotor Blade Flight Loads in Hover and Forward Flight**

Ki C. Kim Survivability/Lethality Analysis Directorate, ARL

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#### 14. ABSTRACT

An aeroelastic analysis was conducted to calculate flight loads on the OH-58D Kiowa Warrior main rotor blade at hover and forward flight conditions. Centrifugal force and flap and chord bending moments were calculated with the University of Maryland Advanced Rotorcraft Code (UMARC) comprehensive helicopter aeroelastic analysis code. The calculated loads were correlated with available flight data for the Bell model 406LM helicopter (model 406T rotor blade) to validate the analytical model. After the correlation study, UMARC was used to calculate blade loads at the ballistic test section radial stations. These baseline loads were represented during the ballistic tests. This report presents the methods and results of the aeroelastic analysis.

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#### 1. Introduction

In support of Kiowa Warrior (KW) main rotor blade ballistic vulnerability tests under the Live Fire Test and Evaluation program (1), a comprehensive helicopter aeroelastic analysis was conducted to calculate flight loads on the OH-58D KW main rotor blade at hover and forward flight conditions. Centrifugal force (CF) and flap and chord bending moments were calculated with the University of Maryland Advanced Rotorcraft Code (UMARC) comprehensive helicopter aeroelastic analysis code (2).

The calculated loads were first correlated with available flight data for the Bell Model 406LM helicopter to validate the analytical model. After the correlation study, UMARC was used to calculate blade loads at the ballistic test section radial stations. These baseline loads were represented during the ballistic tests (1).

The UMARC helicopter aeroelastic model used in the present study is a nonlinear representation of elastic rotor blades coupled to a rigid fuselage. The key feature in UMARC is the use of a finite element (FE) methodology, which can accurately model the kinematics and elastic behavior of the rotating blade. The rotor blade is assumed to be an elastic beam undergoing flap bending, lag bending, elastic twist, and axial deflections. The helicopter fuselage is assumed to be a rigid body undergoing six degrees of freedom. Each blade is modeled as a number of beam FEs. The formulation for the blade and fuselage equations of motion is based on Hamilton's energy principle. The analysis is developed for helicopters with nonuniform rotor blades having pretwist, precone, and chord-wise offsets of the center of mass, aerodynamic center, and tension center, from the elastic axis.

This report presents the methods and results of the aeroelastic analysis. Definitions of symbols used in the report are given in the List of Abbreviations and Symbols. In section 2, the formulation details and aerodynamic model used in UMARC helicopter aeroelastic analysis code are presented. Numerical results are shown and compared with available flight data in section 3. The summary and recommendations for future work are presented in section 4.

### 2. Helicopter Aeroelastic Model

The calculation of rotor loads is a difficult task because of the complex interactions of structural, inertial, and aerodynamic forces acting on the rotary wing. Basically, it is necessary to calculate the periodic aerodynamic and inertial forces of the blade, and thus the resulting motion of structural components. Since the higher harmonic blade loading is the principal source of high loads, an accurate analysis of the rotor aerodynamics is required, including the effects of the

rotor wake, stall, and compressibility. The high frequencies involved and the importance of resonance excitation also require good inertial and structural models.

#### 2.1 UMARC Helicopter Aeroelastic Analysis Code

The UMARC helicopter aeroelastic model used in this study is a nonlinear representation of elastic rotor blades coupled to a rigid helicopter fuselage. The key feature in UMARC is the use of an FE methodology, which can accurately model the kinematics and elastic behavior of the rotating blade. The rotor blade is assumed to be an elastic beam undergoing flap bending, lag bending, elastic twist, and axial deflections. The helicopter fuselage is assumed to be a rigid body undergoing six degrees of freedom. Each blade is modeled as a number of beam FEs. The formulation for the blade and fuselage equations of motion is based on Hamilton's energy principle. The analysis is developed for helicopters with nonuniform rotor blades having pretwist, precone, and chord-wise offsets of the center of mass, aerodynamic center, and tension center from the elastic axis. This code is the current state-of-the-art rotorcraft engineering analysis code and is widely used by U.S. Army Research Laboratory researchers and other Government/industry researchers (e.g., NASA Ames and Boeing and Sikorsky).

In UMARC, aerodynamic loads acting on the rotor blade are calculated using quasi-steady strip aerodynamic theory. Noncirculatory aerodynamic forces are also included. To include the effect of high angle-of-attack flows on the retreating blade, a dynamic stall model is incorporated. Dynamic stall characterizes the delay in flow separation because of unsteady angle of attack and the shedding of a vortex from the leading edge of the airfoil when it gets into a deep stall condition. These effects are introduced in the calculation of section lift and drag and pitching moment. The first step to calculate blade loads and moment is to determine the trim state of the helicopter for given flight conditions (i.e., gross weight, ambient conditions, and forward speed). The UMARC utilizes the coupled trim solution procedure to calculate the helicopter trim in hover and forward flight.

The coupled trim analysis consists of two phases, vehicle trim and steady response, calculated as one coupled solution using a modified Newton's method. For a given flight condition, the control settings and the blade steady response must satisfy both the blade and the vehicle equilibrium conditions. The method of solving simultaneously the blade responses and the trim control settings is referred to as the coupled trim analysis. An uncoupled trim solution based on the rigid flapping blade assumption is used as an initial estimate for the coupled trim analysis. With the trim control settings, the blade steady responses are calculated. Using the blade responses, the rotor hub loads and a new vehicle equilibrium position are recomputed. The control settings are then updated based on the new equilibrium condition (3).

#### 2.2 Vehicle Trim

Propulsive trim, which simulates an aircraft free-flight condition, is used to calculate the initial rotor control settings. The solution is determined from the overall equilibrium—three force (vertical, longitudinal, and lateral) and three moment (pitch, roll, and yaw) equations. (See Kim [4] for more details.)

For a specified helicopter weight coefficient,  $C_w$ , and a forward speed,  $\mu$ , the unknown quantities to be determined from the vehicle equilibrium equations are as follows:

$$u^{T} = \left[\alpha_{s}, \phi_{s}, \theta_{.75}, \theta_{1c}, \theta_{1s}, \theta_{tail}\right]. \tag{1}$$

These values are recalculated iteratively using the modified hub forces and moments, including the blade elastic responses. The solution technique is based on a modified Newton's method. The rotor controls, which are updated at the *i*th iteration, can be expressed in a canonical form as follows:

$$u_{i+1} \cong u_i + \Delta u_i, \tag{2}$$

in which

$$\Delta u_i = -\frac{\partial F}{\partial u}|_{u=u_0} F(u_i), \qquad (3)$$

where  $u_o$  is the trim control settings obtained initially using the rigid flapping blade solution and the Jacobian  $\frac{\partial F}{\partial u}$  is calculated using the finite difference approach. For computational efficiency, the Jacobian is computed only once initially and used for subsequent iterations.

#### 2.3 Rotor Steady Response

The rotor dynamic response involves the determination of time-dependent blade positions at different azimuth locations for one rotor revolution. To reduce computational time, the FE equations are transformed into modal space as a few normal mode equations using the coupled natural vibration characteristics of the blade. These nonlinear periodic coupled equations are solved for steady response using an FE in time procedure based on Hamilton's principle in weak form.

One rotor revolution is divided into a number of azimuthal (time) elements, and then periodicity of response is used to join the motions of the first and last elements. The assembly of elements results in nonlinear algebraic equations that are solved using the Newton-Raphson procedure.

After the blade response is obtained, hub forces and moments are calculated using the force summation method. These values are finally used to recalculate the coupled trim control values, as described in section 2.2.

#### 2.4 Rotor Wake Modeling

For the induced in-flow distribution on the rotor disk, a free-wake model is fully coupled in the rotor aeroelastic analysis. The model can account for wake self-distortion by updating its geometry according to newly calculated in-flow and blade circulation distributions. The geometry of the free wake is divided into the following three regions: (1) near wake, (2) rolling up wake, and (3) far wake. The near wake consists of a series of radial panels, each with linear circulation distributions. The rolling-up wake consists of an inboard linear circulation distribution panel, and a tip panel that represents the rolling up of the tip vortex. The far wake is modeled as one panel with a linear circulation distribution and a concentrated tip vortex whose strength is proportional to the maximum circulation value on the rotor blade. The helical geometry of the concentrated tip vortex is updated, while the inboard wake portions are not changed.

The free-wake analysis is implemented in three stages. First, blade motion and loading are calculated using a linear in-flow model. Next, wake-induced coefficients are calculated for undistorted wake geometry. The nonuniform inflow is calculated and used to obtain blade motion and loading. Finally, the free-wake geometry is calculated. For this, the influence coefficients are reevaluated, and blade motion and loading are again obtained using nonuniform in-flow values. For subsequent iterations, the free-wake geometry is generally held fixed, and only the strength of vortices is updated. This comprehensive rotor wake model is used in the present blade flight loads calculation.

#### 2.5 Solution Procedure for Blade Load Calculations

The following procedures were used to calculate blade loads and moments on selected blade stations in hover and forward flight conditions.

- 1. With prescribed input data, vehicle trim equations are calculated using rigid blade flapping (a starting point).
- 2. Using control inputs from the vehicle trim solution of step 1, the blade nonlinear steady response is calculated. The results give detailed individual blade responses at different span-wise and azimuthal positions.
- 3. Hub loads and moments are calculated using elastic rotor responses. Then, the vehicle trim values and blade responses are recalculated iteratively using the modified hub forces and moments. This step is repeated until a converged solution is obtained.
- 4. Blade loads and moments at selected blade stations are calculated using the force summation method.

#### 3. Results and Discussion

Numerical results are first calculated for the OH-58D KW helicopter at the gross weight of 4500 lb with the forward speed of 120 kn (equivalent advance ratio,  $\mu$ , of 0.28). This flight condition is selected for the benchmark correlation with the available test data obtained on the Bell Model 406T rotor blade (5, 6). The 406T rotor blade is also used on the OH-58D KW. Following the correlation, blade loads were calculated for the KW at a gross weight of 4086 lb for hover and a cruising forward speed of 100 kn ( $\mu$  = 0.23).

The KW helicopter is equipped with a four-bladed, soft in-plane, advanced geometry, hingeless main rotor system. Some important aerodynamic characteristics of this helicopter rotor are given in table 1. In the present study, an effort was made to model the helicopter main rotor blade characteristics as accurately as possible. The rotor blade structural properties data obtained from manufacture (7, 8) were used to create a finite element model (FEM) (see table 2). Figure 1 shows the global and local degrees of freedom of the FE blade model for the whole rotor blade. Nonlinear twist distribution of the blade was also modeled in the blade FEs.

Table 1. Aerodynamic characteristics of KW helicopter.

Air Density, ρ (slug/ft³)	No. of Blades in Main Rotor, N <sub>b</sub>	Helicopter Gross Weight(s), W (lb)	Main Rotor Blade Radius, R (ft)	Blade Tip Speed, ΩR (ft/s)	Blade Mean Chord, c <sub>m</sub> (ft)	Main Rotor Solidity Ratio, σ	Blade Twist, $\theta_{tw}$ (degree)	Rotor Shaft Tilt, $\alpha_s$ (degree) <sup>a</sup>	Blade Precone, $\beta_p$ (degree)	Rotor Disk Area, A (ft²)
$.002378(\rho_{SL})$	4	4500, 4086	17.5	723.88	0.786	0.057	-12	5	2	962

<sup>&</sup>lt;sup>a</sup> Positive for forward tilt.

Table 2. FE beam model input for OH-58D KW main rotor blade.

Element No.	Flap-Wise Bending Stiffness	Lag-Wise Bending Stiffness	Torsional Stiffness	Element Length
	$\left(\frac{EI_{Y}}{m_{o}\Omega^{2}R^{4}}\right)$	$\left(\frac{EI_z}{m_o\Omega^2R^4}\right)$	$\left(\frac{GJ}{m_o\Omega^2R^4}\right)$	$\left(\frac{l_i}{R}\right)$
1(tip)	0.00581	0.02316	0.00522	0.025
2	0.00623	0.04324	0.00634	0.106
3	0.00934	0.06237	0.00935	0.169
4	0.00823	0.05762	0.00843	0.100
5	0.01420	0.08321	0.01743	0.152
6	0.02342	0.16342	0.02654	0.162
7	0.03429	0.32143	0.03021	0.086
8 (root)	0.22840	0.72342	0.06443	0.084

For the calculation of blade dynamic response, each rotor blade is discretized into eight beam elements, and each beam element consists of 15 nodal degrees of freedom (see figure 1). For normal mode reduction, five coupled rotating natural modes comprised of two flaps, two lags, and one torsion mode are used. For periodic response, one cycle of time is discretized into eight time elements, and each time element represents a fifth-order polynomial distribution of motion.

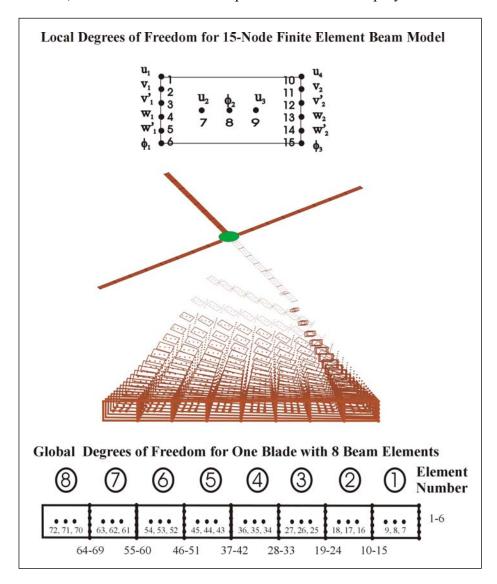


Figure 1. Local and global degrees of freedom of KW main rotor blade.

Figure 2 shows the correlation of the blade rotating natural frequencies. The UMARC calculated values are compared with the experimental data (7) obtained on the Bell 406 helicopter rotor blade. The UMARC results are calculated with the nominal operating rotational value of 395 rpm. There is a good correlation between the analytical UMARC results and the experimental data, especially for the lower modes. It is also seen that UMARC slightly underpredicts the torsional frequency.

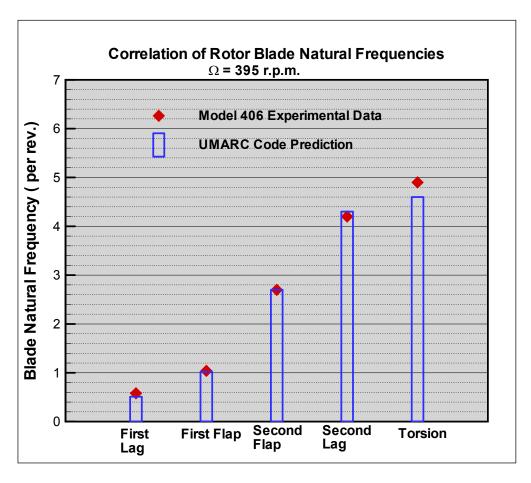


Figure 2. Correlation of main rotor blade natural frequencies.

#### 3.1 Correlation Study

To validate the current blade load analysis, the calculated blade centrifugal loads and bending moments were compared with available flight test data. The correlation study will not only serve as an analysis check, but also as a guideline for further UMARC model improvement efforts.

Figure 3 shows the correlation of the centrifugal force acting on the blade stations. The UMARC calculated values are compared with the flight test data obtained on the Bell 406 helicopter. The centrifugal forces measured during the flight test are available at the two blade stations— 26,600 lb at inboard blade station 24.25 (r/R = 0.116) (5) and 20,600 lb at outboard blade station 96 (r/R = 0.457) (6). Comparing the UMARC results obtained using nonuniform FE beam model with the flight test data, we observe an excellent correlation. Also shown in the figure is the analytical result obtained with a simple uniform blade assumption. As expected, the result obtained using the uniform blade shows a poor correlation. This is most likely due to the high nonuniformity of the helicopter blade; rotor analysis with a simple uniform blade model can generate erroneous results.

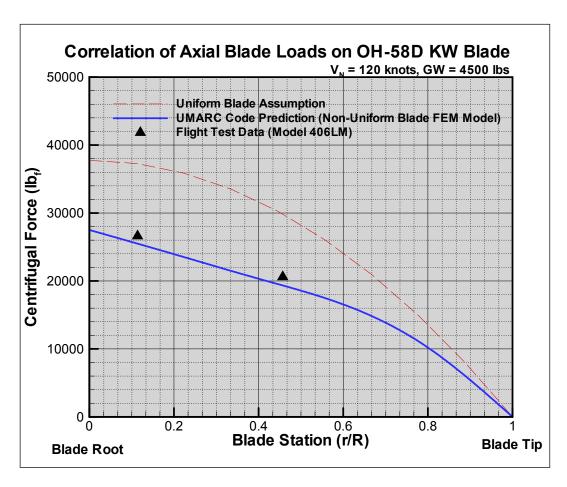


Figure 3. Correlation of CFs along the blade span.

The computed blade bending moments were also correlated with the flight test data. In reference (5), three flap bending moment values are given at three inboard blade stations—stations 31 (r/R = 0.148), 40 (r/R = 0.191), and 50 (r/R = 0.238), respectively. In reference (6), only one bending value is given at the outboard blade station 96 (r/R = 0.457). These flight values were replicated and shown in table 3. Also, shown in the fourth column of the table are the peak-to-peak values of the moments. The peak-to-peak value is a good indication of loading on the structural component. It is seen that the bending moment is largest inboard and decreases outboard.

Figure 4 shows the correlation of the UMARC flap-bending moments with the flight test data. There are some discrepancies between the UMARC results and the flight test data. However, considering the complexities associated with rotor loads and vibration analysis, a reasonably good agreement is observed. In particular, the general trend and the peak-to-peak magnitude of the moments are well correlated with flight test data, especially at inboard blade stations.

Table 3. Flap bending moments of Bell model 406T helicopter main rotor blade.

Blade Station (r/R)	Mean Value (in-lb <sub>f</sub> )	Oscillatory Value (in-lb <sub>f</sub> )	Peak-to-peak Value (in-lb <sub>f</sub> )
0.148	2125	±2725	5450
0.191	1725	±2360	4720
0.238	1275	±2000	4000
0.457	-180	±780	1560

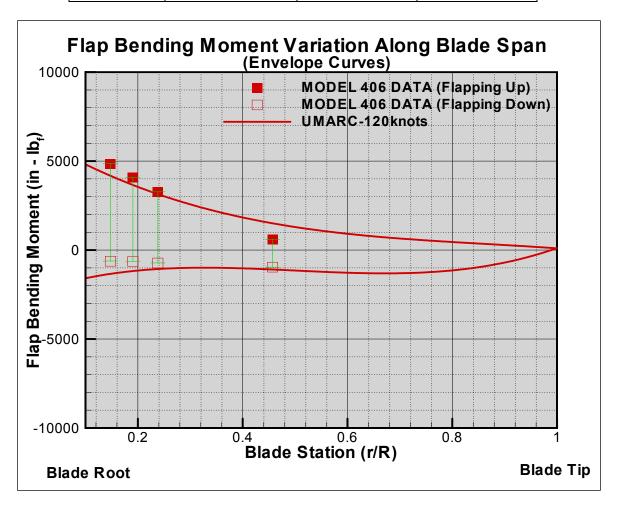


Figure 4. Correlation of flap bending moment along blade span ( $\mu = 0.28$ ).

Figure 5 shows the correlation of UMARC lag bending moments with flight test data. Again, there are some discrepancies between the analytical results and the test data. A comparison reveals that the UMARC values are slightly greater than the test data values. However, a reasonable correlation with the test data is observed, and the general trend is especially well correlated.

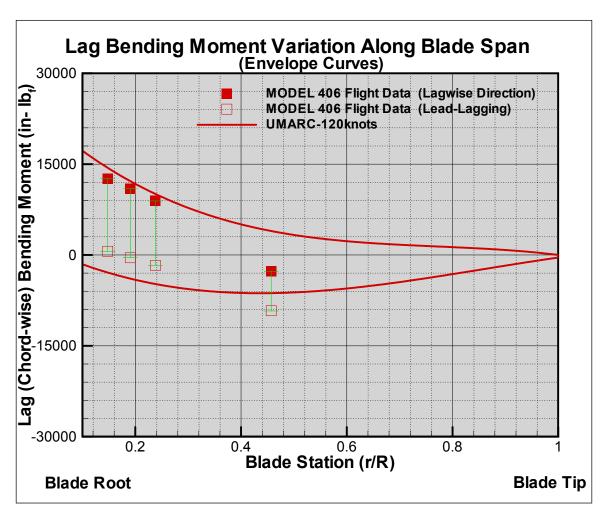


Figure 5. Correlation of lag bending moments along blade span ( $\mu = 0.28$ ).

Next, the UMARC calculated blade torsional moments were correlated with the flight test data in Figure 6. There are only two blade stations where the flight torsional data are available—the inboard blade station 24.25 (r/R = 0.116) (5) and the outboard blade station 96 (r/R = 0.457) (6). The inboard station (r/R = 0.116) is where the main rotor blade is connected with the pitch link. Again, there are some discrepancies between the two results. However, a reasonable correlation is observed.

#### 3.2 Blade Flight Load Calculations for Hover and 100-kn Forward Speed

From the correlation study, it was determined that the UMARC code adequately calculated flight loads. Excellent agreement with test dada was observed for the most dominant loading (i.e., the axial load), giving a certain confidence in the helicopter rotor subsystem model. Next, a new set of bending moments was calculated for the ballistic test flight conditions—the gross weight of 4086 lb at hover and a cruising forward speed of 100 kn ( $\mu$  = 0.23) for three blade radial

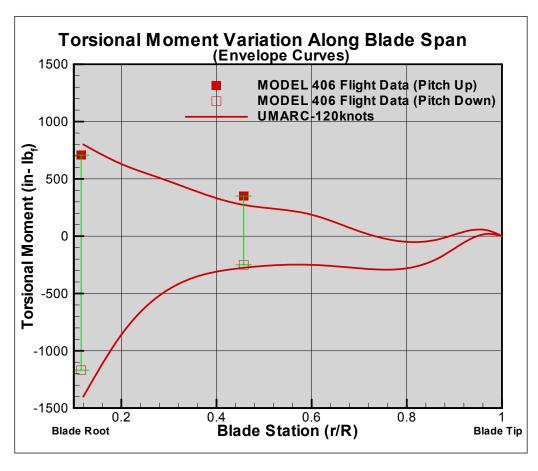


Figure 6. Correlation of torsional moments along blade span ( $\mu = 0.28$ ).

stations. Since the new flight conditions had a negligible influence on the centrifugal force on the blade, the previous calculated values were used for the axial loading. These loads and moments (peak values) were used as baseline loads during the ballistic test events. The results are summarized in table 4.

Table 4. Reference blade loads and moments for test phase I-B.

		FB	FB	FB	LB	LB	LB
Blade		Hover	100 kn	120 kn	Hover	100 kn	120 kn
Station	CF	GW = 4086 lb	GW = 4086 lb	GW = 4500 lb	GW = 4086 lb	GW = 4086 lb	GW = 4500 lb
(r/R)	(lb)	(lb-in)	(lb-in)	(lb-in)	(lb-in)	(lb-in)	(lb-in)
0.286	22374	2020	2219	2691	6860	7605	8284
0.614	16220	564	795	872	1416	1743	2169
0.843	8264	202	242	379	684	690	1112

Notes: FB = flap bending moment, positive flapping up; LB = lag (chord-wise) bending, positive lagging back.

### 4. Summary

An aeroelastic analysis was conducted to calculate flight loads on the OH-58D KW main rotor blade for hover and cruise forward-flight conditions. Centrifugal force and flap and lag bending moments were calculated using the UMARC code. The calculated loads were correlated with flight test data for the Bell model 406LM helicopter to validate the analysis. The correlation showed good general agreement between the test data and analytical results. After the correlation study, blade loads were calculated for the desired ballistic test conditions.

In the present study, the UMARC comprehensive helicopter aeroelastic analysis, based on FE methodology in both space and time coordinates, was conducted to analytically calculate the flight loads. In spite of it being computer-intensive, its benefit must be appreciated as a powerful analytical tool to validate simple design-oriented analysis.

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## **List of Abbreviations and Symbols**

A	Rotor disk area, $\pi R^2$
$c_{ m m}$	Mean blade chord length
$C_W$	Helicopter weight coefficient, $\frac{W}{\rho A(\Omega R)^2}$
E	Young's modulus
$EI_{v}$	Effective flap bending stiffness
$\mathrm{EI}_{\mathbf{z}}$	Effective lag (chord) bending stiffness
G	Shear modulus
GJ	Effective sectional torsion stiffness
$I_y, I_z$ $J$	Blade cross-sectional moment of inertia about y and z axis, respectively
J	Polar moment of inertia
$l_{i}$	Length of the <i>i</i> th beam element
$m_o$	Reference blade section mass
$N_b$	Number of rotor blades
$R_{_{\mathrm{T}}}$	Blade radius
$u^{\mathrm{T}}$	Row vector of unknowns in vehicle trim equations
u	Blade displacement in the axial direction
V	Helicopter forward speed
V	Blade displacement in the lead-lag direction
W	Helicopter weight
W	Blade displacement in the flap-wise direction
$\alpha_{\mathrm{s}}$	Longitudinal shaft tilt
$\theta$ .75	Main rotor collective pitch angle at 75% blade radius
$\theta_{1c}, \theta_{1s}$	Lateral and longitudinal cyclic trim pitch angles, respectively
$\Theta_{ ext{tail}}$	Tail rotor collective pitch angle at root
μ	Advance ratio, $\frac{V}{\Omega R}$
σ	Rotor solidity ratio, $\frac{N_b c_m}{\pi R}$
ф	Elastic blade twist about the elastic axis
$\phi_{\rm s}$	Lateral shaft tilt
ρ	Air density
Ω	Rotor rotational speed

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#### ABERDEEN PROVING GROUND

20 DIR USARL

AMSRD ARL SL B

AMSRD ARL SL BB

D JORDAN

M KUNKEL

S MOULSDALE

B WALTHER

AMSRD ARL SL BD

S POLYAK

B SMITH

J FRIES

D TEN BROECK

K KIM (10 CPS)

AMSRD ARL SL BE

E FIORAVANTE